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EVALUATING OAK ADVANCE REPRODUCTION IN THE MISSOURI OZARKS

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APPLICATION

This guide presents a method for determining in advance of final harvest whether reproduction is adequate to reasonably ensure the regeneration of an oak stand. The guide is based on studies of survival and growth of oak reproduction on a range of sites from site index 50 to 70 for black oak in the Missouri Ozarks. The guide assumes oaks will be grown in even-aged stands as recommended by Roach and Gingrich (1968) and Sander (1977).

The guide requires inventories of (a) the overstory and (b) the oak advance reproduction. Both inventories should be made at the same time and tallied on a form (fig. 1). If the oak advance reproduction inventory shows there are insufficient oaks to replace the stand, the overstory inventory is used to determine whether or not stump sprouts from overstory oaks are likely to be numerous enough to make up for deficiencies in advance reproduction.

To Use This Guide

1. Tally all oaks 1.6 inches d.b.h. and larger on 10 or more 1/20-acre plots by species and size classes (overstory inventory, see sample form (fig. 1)).

2. Determine average age of dominant and codominant oaks and site index from tables in Appendix II and record on the tally form. Also determine and record the average age of lower story (intermediate and suppressed) oaks that are 1.6 inches d.b.h. and larger.

3. Select the number of 1/735-acre plots (4.3 feet in radius) to use in the advance reproduction inventory from the following tabulation according to the acreage of the stand being examined:

For stand size (Acres)	Use this number of 1/735-acre plots
<10	25
10-30	40
30-50	60

4. Distribute these 1/735-acre plots uniformly throughout the stand.

5. Measure the tallest stem of advance oak reproduction on each 1/735-acre plot and record (advance reproduction inventory (fig. 1)). Tally these stems by 2-foot height classes and 1/2-inch ground diameter classes (table 1). A 6-inch caliper graduated in either tenth or quarter inches can be used for measuring ground diameters. Measure only trees 1.5 inches d.b.h. or less; stems larger than this should be considered part of the overstory and tallied as such, even if below the main canopy. If no oak advance reproduction is present, record zero for height and ground diameter on the tally form.

6. Record on the advance reproduction tally form the aspect of each plot by quadrant (NE, SE, SW, or NW) and its slope position (upper, middle, or lower thirds). For plots on level topography (all slopes less than 15 percent), narrow ridge tops, or bottoms, code as LE, RI, or BO, respectively, under slope position and use the stocking values for southeast/northwest aspects (table 1).

7. Determine the stocking value (SV) for each plot by referring to table 1 and record on the tally form. Then calculate the average SV and round off to the nearest whole number. If average SV is 30 percent or greater, oak advance reproduction is adequate; no further calculations are necessary and the stand can be harvested.

8. If the average SV is less than 30 percent, oak advance reproduction is inadequate to reproduce the stand if it is cut. But the stand can still be reproduced if enough stumps of the overstory oak trees will sprout after they are cut. To compute the contribution to reproduction stocking from expected stump sprouting:

- Assume that the inventory of plots provides the data on the sample form (fig. 1).
- Note that there are 26 black oaks 2 to 5 inches in diameter per acre. Multiply 26 by 0.42 (from table 2) to find how many of the 26 stumps are expected to produce codominant or dominant trees at age

Date 9/12/83 Compartment 1 Stand 10 Site Index 60

Stand Age(Dominants) 80 Stand Age(Lower story) 80

Overstory (1/20-acre plots)							Advance Reproduction (1/735-acre plots)										
Sample Point Number	D.B.H. Class	Black Oak	White Oak	Scarlet Oak	N. Red Oak	Other Spp.	Plot No.	Asp.	Slope Pos.	Ht.	Grnd. Dia.	SV					
1	2-5	..	..	.		..	1	SE	LO	0	0	0					
	6-11		.			.	2	SE	LO	10	2.0	38					
	12-16					.	3	SE	LO	0	0	0					
	17+				.		4	SE	LO	2	.5	2					
2	2-5	..	..				5	SE	LO	2	.5	2					
	6-11	.	.			..	6	SE	LO	0	0	0					
	12-16		.				7	SE	LO	6	1.5	23					
	17+						8	SE	LO	4	.5	4					
3	2-5	.	.	..		.	9	SE	LO	8	1.5	28					
	6-11			.			10	SE	LO	0	0	0					
	12-16		.			.	11	SE	LO	6	.5	8					
	17+						12	SE	LO	0	0	0					
4	2-5		..			..	13	SE	LO	2	.5	2					
	6-11						14	SE	MI	4	.5	18					
	12-16	..		.		..	15	SE	MI	8	1.5	73					
	17+						16	SE	MI	4	.5	18					
5	2-5		..	..			17	SE	MI	8	1.5	73					
	6-11	.	..				18	SE	MI	0	0	0					
	12-16						19	SE	MI	4	1.0	37					
	17+		.				20	SE	MI	1	-	2					
6	2-5	.	..	..		..	21	SE	MI	8	1.0	64					
	6-11					.	22	SE	MI	0	0	0					
	12-16	..	.			.	23	SE	MI	6	1.5	65					
	17+						24	SE	MI	4	1.5	56					
7	2-5	..	..	..			25	SE	MI	8	1.5	73					
	6-11		.			..	26	SE	MI	0	0	0					
	12-16					.	27	SE	UP	10	2.0	79					
	17+	.					28	SE	UP	0	0	0					
8	2-5	..	.	.	..	..	29	SE	UP	0	0	0					
	6-11	.					30	SE	UP	8	1.5	68					
	12-16	.			.		31	SE	UP	1	-	1					
	17+						32	SE	UP	10	2.0	79					
9	2-5		..			..	33	SE	UP	0	0	0					
	6-11	.			.	.	34	SE	UP	0	0	0					
	12-16	..	.	.		.	35	SE	UP	6	1.5	59					
	17+						36	SE	UP	0	0	0					
10	2-5	..	..	.			37	SE	UP	0	0	0					
	6-11		.		.	.	38	SE	UP	8	1.5	68					
	12-16	..					39	SE	UP	6	1.5	59					
	17+						40	SE	UP	1	-	1					
Total No. Per Acre	2-5	26	60	24	4	26	140	SV Mean				25					
	6-11	8	12	2	4	22	48										
	12-16	18	8	4	2	14	46	Advance Reproduction Adequate?				No					
	17+	2	2	0	2	0	6										
No. of Stump Spts. Per Acre	Total	54	82	30	12	62	240	Advance Reproduction + Stump Sprouts Adequate?				Yes					
	2-5	11	11	11	2	X	Total Per Acre										
	6-11	1	1	2	2												
	12-16	1	0	2	1												
	17+	0	0	0	0												
Total	13	12	15	5		45											

Figure 1.—Example tally form for recording overstory trees and oak advance reproduction stocking and for computing the number of expected oak stump sprouts.

Table 1.—*Stocking value¹ for advance reproduction inventory plots*

Size of tallest tree per plot		Aspect and slope position of plot								
Height class (ft)	Ground diameter class	Southwest			Southeast & Northwest			Northeast		
		Upper	Middle	Lower	Upper	Middle	Lower	Upper	Middle	Lower
≤ 1	In. All	1	1	0	1	2	0	1	1	0
2	0.5 (0.3-0.7)	5	6	1	8	9	2	4	5	1
(1.1-3.0)	1.0 (.8+)	14	17	3	22	26	6	13	15	3
4	0.5 (.3-.7)	10	11	2	15	18	4	8	10	2
(3.1-5.0)	1.0 (.8-1.2)	22	25	6	32	37	9	19	22	5
	1.5 (1.3+)	37	42	11	51	56	18	34	38	10
6	0.5 (.3-.7)	19	22	5	28	32	8	16	19	4
(5.1-7.0)	1.0 (.8-1.2)	32	36	9	45	50	14	29	33	8
	1.5 (1.3+)	45	50	15	59	65	23	41	46	13
8	1.0 (.8-1.2)	44	49	14	59	64	22	40	45	12
(7.1-9.0)	1.5 (1.3-1.7)	54	59	19	68	73	28	49	54	17
	2.0 (1.8+)	62	67	24	76	80	35	57	62	21
10+	1.0 (.8-1.2)	58	63	22	72	77	32	54	59	14
(9.1+)	1.5 (1.3-1.7)	62	67	24	76	81	35	58	63	16
	2.0 (1.8-2.2)	66	71	27	79	84	38	61	66	19
	2.5 (2.3+)	69	74	29	82	86	41	64	69	21
Narrow ridge tops -----										
Level areas (<15 percent slopes other than ridge tops and bottoms) -----										
Bottoms -----										

¹Stocking Value (SV) is the contribution of a single stem to stand stocking at age 20.

20: $26 \times 0.42 = 11$ (rounded off to the nearest whole number). The expected number of stump sprouts per acre for 2- to 5-inch black oaks, 11, is listed at the bottom of figure 1.

- c. Similarly, compute the expected number of stump sprouts for the other size classes of black oak (1 for the 6- to 11-inch class, 1 for the 12- to 16-inch class, and 0 for the 17+ inch class) and note that all these classes sum to 13. Do the same for all oak species.
- d. Summing all oak species and all size classes gives a total of 45 expected stump sprouts per acre (fig. 1).

9. Go to table 3 and find the number of stump sprouts required in combination with advance reproduction stocking to meet minimum stocking requirements. Opposite 25 note that 37 stump sprouts are needed to make up the deficiency in advance reproduction. (Suppressed and intermediate oaks (particularly white oaks) may be younger than the stand dominants. Thus if 2- to 5-inch white oaks had been 40 years old instead of 80, expected stump sprouts from this diameter class would be 37 per acre—sufficient by themselves to compensate for the deficiency in advance reproduction. Consequently, the average age of lower story oaks should always be determined.)

10. Because the computed value (45) exceeds the tabulated value (37), oak stump sprouts will make up for deficiency in the advance reproduction. Thus, the oak component of the new stand will be adequate and the old stand can be harvested.

11. If the number of expected stump sprouts does not compensate for advance reproduction deficiencies, harvesting should be delayed until adequate oak advance reproduction is established. The alternative is to plant oak seedlings (Johnson [in prep.]).

12. To determine oak regeneration potential more rapidly, a program for Hewlett-Packard¹ programmable calculator is presented in Appendix III.

¹Mention of trade names does not constitute endorsement of the products by the USDA Forest Service.

Table 2.—Expected proportion of stumps that will produce, at probability 0.8 or greater, at least one codominant or larger stem at age 20

Species	Site index	D.b.h. class	Age of parent tree (years)				All ages
			40	60	80	100	
		<i>ln</i>					
Black oak ¹	50	2-5	0.36	0.34	0.32	0.30	—
		6-11	.13	.11	.10	.08	—
		12-16	.06	.05	.04	.03	—
		17+	—	.02	.02	.01	—
	60	2-5	.47	.45	.42	.40	—
		6-11	.16	.15	.13	.12	—
		12-16	.07	.06	.05	.04	—
		17+	—	.03	.02	.02	—
	70	2-5	.61	.59	.56	.54	—
		6-11	.21	.19	.17	.16	—
		12-16	.10	.08	.07	.06	—
		17+	—	.05	.04	.03	—
White oak ¹	50	2-5	.47	.25	.12	.05	—
		6-11	.18	.10	.06	.03	—
		12-16	.06	.04	.03	.02	—
		17+	—	.02	.01	.01	—
	60	2-5	.63	.38	.19	.08	—
		6-11	.26	.16	.09	.05	—
		12-16	.09	.07	.05	.03	—
		17+	—	.03	.02	.02	—
	70	2-5	.81	.55	.31	.15	—
		6-11	.36	.25	.16	.09	—
		12-16	.15	.11	.08	.06	—
		17+	—	.05	.04	.04	—
Northern red oak ²	60+	2-5	.86	.86	.49	.49	—
		6-11	.86	.86	.46	.46	—
		12-16	.86	.86	.38	.38	—
		17+	—	.86	.24	.24	—
Scarlet oak ³	50+	2-5	—	—	—	—	0.46
		6-11	—	—	—	—	.96
		12-16	—	—	—	—	.46
		17+	—	—	—	—	.10

¹Values are based on data from Johnson (1977).

²Values are based on data from Wendel (1975) and Johnson (1975).

³Values by parent tree age are not available. Values given are means for sawtimber-size stands of various but unknown ages.

Table 3.—Number of stump sprouts required to compensate for stocking deficiencies of advance reproduction

Mean stocking value (SV) for 1/735 - acre plots	Stump sprouts required Number per acre
≥30	0
29	8
28	15
27	23
26	30
25	37
24	45
23	52
22	59
21	67
20	74
19	81
18	89
17	96
16	103
15	111
14	118
13	125
12	133
11	140
10	148
9	155
8	162
7	170
6	177
5	184
4	192
3	199
2	206
1	214
0	221

DOCUMENTATION

Background

In even-aged stands, the oak component after final harvest cutting depends on size, number, and distribution of the oak advance reproduction (Sander 1971, 1972; Sander and Clark 1971). However, oak advance reproduction numbers differ greatly under mature stands. In the Missouri Ozarks, the number may range from less than 300 to more than 2,000 stems per acre.² Some of this variation is attributable to site

quality—in general, oak advance reproduction is more abundant on average and poor sites than on good sites (Sander and Clark 1971).

Abundance of oak advance reproduction alone is not a good indicator of whether or not oaks will be a major component of a new stand after final harvest cutting. This is because much of the reproduction may be too small to successfully compete with associated vegetation. Thus, tree size, as well as tree numbers, should be considered in evaluating the oak regeneration potential.

Variation in oak advance reproduction size is related to recurrent stem dieback, which results in predominantly seedling-sprout populations in Ozark oak forests. Consequently, the root systems of large seedling-sprout reproduction are much older than the stems and are able to support much greater stem growth than recently established seedlings and small seedling-sprouts.

Both stem height and basal diameters of oak advance reproduction are related to growth after overstory removal (McQuilkin 1975, Sander 1971). Thus both height and diameter are indicators of total plant size and the potential of the root systems to support vigorous shoot growth after overstory removal.

Estimating fifth-year "success" probabilities.—To determine the relation between oak advance reproduction size and development after overstory removal, we measured 394 stems in 6 stands in the Missouri Ozarks before and after clearcutting. Eighty-five percent of these stems were black oak (*Quercus velutina* Lam.) and white oak (*Q. alba* L.) and the remainder were scarlet oak (*Q. coccinea* Muenchh.) and northern red oak (*Q. rubra* L.). These trees were well distributed across all aspects and slope positions in stands with black oak site index 50 to 70 (McQuilkin 1974).

We chose oak stump sprouts as the standard for determining oak reproduction success because of their rapid growth and predominance in the upper crown strata of these 5-year-old stands. We defined a "successful" oak as one that had attained at least 80 percent of the mean height of all oak stump sprouts measured. These stump sprouts averaged 11 feet tall at age 5 so to be "successful" an oak had to be at least 8.8 feet tall. Eighty percent was chosen as the success criterion because nearly all oaks at least 8.8 feet tall at age 5 were dominant or codominant. Using this criterion for success and initial and 5 year measurements, we developed equations for predicting the probability of success for an individual stem of a given size using logistic regression analysis (Engelman 1981). In addition to initial tree height and basal

diameter, we used aspect and slope position to predict success probability (Appendix I). These success probabilities did not differ significantly by species ($P < 0.05$) so the resulting estimates are for all four species combined.

The regression estimates showed that success probabilities increase with increasing initial height and ground diameter. In addition, probabilities were highest on southeast and northwest aspects and on middle slope positions. Initial size being equal, probabilities of success were lowest on northeast facing slopes and on lower slope positions. Probabilities of success ranged from less than 0.01 for 1-foot tall trees of small diameter on lower slopes to 0.88 for trees 10 feet tall with large (2.5-inch) ground diameters on middle slopes of southeast or northwest aspects. In general these relations reflect a low likelihood of tree development in environments where soil moisture is extremely favorable or unfavorable. This relation may in turn be related to high mortality and/or poor growth on droughty sites and severe competition on moist sites.

Establishing A Future Stocking Goal

Determining the minimum amount of oak advance reproduction for adequate stocking in a new stand requires first defining "adequate stocking." At some future stage of stand development enough dominant and codominant oaks must be in the stand to furnish some minimum stocking level. The stage chosen for this guide is when the mean stand diameter is 3 inches. The goal we've selected is to have the stand at least 30 percent stocked (C level) with codominant and dominant oaks at this mean stand diameter. Total stand stocking will be higher because trees of other species and probably some smaller oaks will be present.

Unmanaged oak stands on average sites (black oak site index 60-75) in a Missouri study reached a mean stand diameter of 3 inches at age 20 to 25, and the dominant and codominant trees averaged 4.5 inches in diameter². According to Gingrich's (1967) equation for defining minimum tree area requirements, one 4.5-inch tree contributes 0.136 percent stocking and requires 1.36 milacres of growing space. To attain the 30 percent stocking goal requires $30/0.136$ or 221 trees averaging 4.5 inches in diameter when the mean stand diameter is 3 inches.

Estimating the Contribution of Advance Reproduction to Future Stand Stocking

Advance reproduction's contribution to future stand stocking depends on its future utilization of growing space. This is generally not practical to measure until the stand reaches a mean stand diameter of 3 inches—the lowest mean diameter shown on Gingrich's (1967) stocking chart. Because this occurs at about age 20, we extended fifth-year success probabilities (P_5) to age 20 to estimate the advance reproduction contribution. We assumed a 1 percent per year loss of trees deemed successful the fifth year to mortality and suppression over the next 15 years (Sander *et al.* 1976). The resulting probabilities (P_{20}) are thus estimates of the proportion of advance reproduction stems expected to be codominant or dominant at age 20.

Given these probabilities (P_{20}), we then determined the number of oak advance reproduction stems (R) required to produce, at probability 0.8 or greater, at least one codominant or larger stem at age 20 by using the following relation based on the binomial probability distribution:

$$R = \log(1-0.8)/\log(1-P_{20}) \quad (1)$$

(Johnson 1976, Leak 1969). We selected 0.8 as a "confidence" probability because, it is a compromise between excessively high stocking requirements resulting from the use of a higher confidence probability on the one hand and an unacceptably low confidence in P_{20} on the other hand. The probability that one advance reproduction stem of a given size becomes codominant or larger 20 years after final harvest at least 80 percent of the time is then $1/R$. Expressed as a percent, $1/R$ is referred to as a stocking value (SV) because it defines the contribution of a stem to future stand stocking and can be used to quantify the stocking of an individual plot.

The average stocking value for a stand based on an inventory using 1/735-acre plots is the percent of the 735 growing spaces expected to produce codominant or dominant oaks at a mean stand diameter of 3 inches (about age 20). This percent must then equal or exceed 30 (i.e., $(221/735)100$) for oak advance reproduction to be adequate and fulfill minimum future stocking requirements based on the 221 tree goal.

Sample Plot Size and Number

The appropriate unit for sampling oak advance reproduction should be related to the average size (4.5 inches d.b.h.) of dominant and codominant trees when the mean stand diameter is 3 inches. A 4.5-inch tree requires 1.36 milacres or 1/735-acre of growing space. Theoretically, then, on any given acre the opportunity exists for each 1/735-acre to contain one 4.5-inch tree. At or beyond a mean stand diameter of 3 inches, more than one codominant or larger tree would not be expected to persist within this sample space. Thus the appropriate plot size is 1/735-acre (4.3-foot radius).

The number of 1/735-acre plots shown on page one is a reasonable estimate of the minimum number of sample plots needed for inventorying advance reproduction. If greater precision is desired, a preliminary sample should be used to estimate confidence limits and the required number of plots for a given level of precision should be calculated based on the binomial distribution (Freese 1962).

THE ROLE OF STUMP SPROUTS

The potential for sprouting from stumps of over-story oaks can be used to compensate for deficiencies in oak advance reproduction when evaluating the oak reproduction potential of a stand. Stump sprouts are the fastest growing oak component in new stands and those of low origin generally develop into good quality trees.

Factors shown to influence oak stump sprouting in a Missouri study include parent tree age and d.b.h. and site quality. Sprouting frequency decreases with both increasing parent tree age and d.b.h. but increases with increasing site quality. These relations were used to develop equations to estimate the proportion of parent trees that would produce codominant or larger black, white, and scarlet oaks at age 5 (Johnson 1977). These proportions were adjusted for anticipated mortality to stand age 20 by assuming a population reduction of 0.75 percent per year for 15 years. This adjustment was based on a 32-year stump sprout study (Roth and Hepting 1969). Data from Wendel (1975) and Johnson (1975) were similarly used to estimate proportions for northern red oak.

Using these adjusted proportions, values of R were calculated by using equation (1); $1/R$ was then used as the estimate of the proportion of parent trees expected to produce, at probability 0.8 or greater, at least one codominant or larger stem at age 20 (table 2). For black oak and white oak, expected proportions are shown by parent tree age, parent tree d.b.h., and site index. Age and site index information were not available for scarlet oak, so proportions are given by

diameter classes only. The latter values are averages for sawtimber-size stands in the Missouri Ozarks. Proportions for northern red oak are based on data from parent stands in West Virginia that were 50- to 55-years-old on site index 60 to 80, and from stands in Wisconsin that ranged from about 70- to 110-years-old on site index 50 to 70 (Wendel 1975, Johnson 1975). Season of cutting may also influence stump sprouting and subsequent sprout development (Wendel 1975, Clark and Liming 1953), so we took this into account when determining these probabilities.

The minimum number of stump sprouts per acre (N) required to compensate for deficiencies in advance reproduction is:

$$N = 221 - \bar{SV}(7.35),$$

where $\bar{SV}$ is the mean stocking value for oak advance reproduction obtained by applying stocking values for advance reproduction inventory plots (table 1) to an inventory of 1/735-acre plots (table 3). This minimum number of trees can then be compared to the estimated number of expected stump sprouts to determine if advance reproduction plus stump sprouts will be adequate to replace the old stand.

IN CONCLUSION

The guide presents a method for obtaining "best available" estimates of the regeneration potential for Ozark oak forests based on currently available information. How well the guide works can be determined only by how many oaks grow fast enough to maintain themselves in a good competitive position as the stand develops. We used data from six Missouri Ozark stands to make a small test of the guide's ability to predict "success." Based on the number of oaks per acre at least 8 feet tall at age 5 the guide predicted "success" correctly in 5 of the 6 stands.

We hope silviculturists will apply the guide conscientiously and test its validity by inventorying reproduction at periodic intervals after harvest cutting. We hope users will share their results with us. In this way we can be made aware of the guide's shortcomings or strengths and what revisions may be needed. It will be revised as experience in application and new information dictates.

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APPENDIX I.

Regression coefficients for the equation for estimating fifth-year success probabilities (P5) for oak advance reproduction¹

Independent variable	Regression coefficient (B) ²
X1: Square root of tree ground diameter (in)	5.10
X2: Total tree height (ft)	0.700
X3: X1 x X2	-0.444
X4: Log(success criterion) ³	-5.95
X5: Aspect(V1) ⁴	-0.284
X6: Aspect(V2) ⁴	0.404
X7: Slope position(V1) ⁵	-1.10
X8: Slope position(V2) ⁵	0.646
Constant (B ₀)	19.0

¹The equation is of the form:

$$P5 = 1 + \exp[-B_0 + B_1X_1 + \dots B_nX_n]^{-1},$$

where P5 is the probability that an individual stem of oak advance reproduction will attain or exceed the success criterion set by the value of X4.

²All regression coefficients are significant at the 0.01 level. Goodness of fit was also evaluated by chi-square (Engelman 1981). Total number of observations in the regression data set was 2,364.

³X4 = the natural logarithm of the selected success criterion (a percent). We solved the equation for a success criterion of 80, i.e., 80 percent of mean stump sprout height at age 5. At that age stump sprouts averaged 11 feet tall, and those that were 80 percent or more of that height (i.e., at least 8.8 feet tall) were usually codominant or dominant and thus "successful". However, the equation can be solved for any success criterion (e.g., 70 or 90 percent).

⁴X5 and X6 are vectors (V) of the independent variable "aspect" that *jointly* express the aspect effect on the estimate of P5. Coded values of X for both vectors are given below for the four aspects considered.

Aspect	Value of X for vector	
	Aspect(V1)	Aspect(V2)
SW	-1	-1
SE and NW	0	1
NE	1	0

⁵X7 and X8 are vectors (V) of the independent variable "slope position" that *jointly* express the slope position effect on the estimate P5. Coded values of X for both vectors are given below for the three slope positions considered.

Slope position	Value for X for vector	
	Slope position(V1)	Slope position(V2)
Upper third	-1	-1
Middle third	0	1
Lower third	1	0

To simplify application, we used categorical values of aspect and slope position instead of continuous values such as degrees azimuth and percent of distance from the ridge. The values of these categorical variables are based on "effects" coding and are generated by the logistic regression program (Engelman 1981); the statistical properties of the resulting coefficients are discussed by Kerlinger and Pedhazur (1973, pp. 121-128).

APPENDIX II.— Determining Site Index

1. Select at least 5, preferably 10, straight undamaged dominant or codominant trees per stand that show no signs of suppression. Selected trees should not differ more than 5 years in age from the trees immediately surrounding them.
2. Measure tree height and breast-height age; add 2 years to breast-height age to get total age.
3. Calculate average height and age and look up site index in tables 4 and 5.
4. Approximate conversions between species may be made as follows:

Black oak SI = Scarlet oak SI-3

Black oak SI = White oak SI+4

Scarlet oak SI = Black oak SI+3

White oak SI = Black oak SI-4.

Table 4.--Black and scarlet oak site index estimates by 2-foot height and 2-year age intervals^{1/} (McQuilkin 1974)

Age (years)	8:10:12:14:16:18:20:22:24:26:28:30:32:34:36:38:40:42:44:46:48:50:52:54:56:58:60:62:64:66:68:70:72:74:76:78:80:82:84:86:88:90:92
10	55 57 59 61 63 64 66 68 70 72
12	54 56 58 60 62 63 65 67 69 71
14	53 55 57 59 61 62 64 66 68 70 72 74
16	52 54 56 58 60 62 63 65 67 69 71 73 75
18	51 53 55 57 59 60 62 64 66 68 70 72 74 76 78
20	50 52 54 56 58 60 61 63 65 67 69 71 73 75 77 79
22	49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
24	48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
26	47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
28	46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
30	45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
32	44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
34	43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
36	42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
38	41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
40	40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
42	39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
44	38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
46	37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
48	36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
50	35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
52	34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
54	33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
56	32 34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
58	31 33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
60	30 32 34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
62	29 31 33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
64	28 30 32 34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
66	27 29 31 33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
68	26 28 30 32 34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
70	25 27 29 31 33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
72	24 26 28 30 32 34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
74	23 25 27 29 31 33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
76	22 24 26 28 30 32 34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78
78	21 23 25 27 29 31 33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69 71 73 75 77
80	20 22 24 26 28 30 32 34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68 70 72 74 76 78

^{1/} All height and age combinations in this table are within the range of the original black oak data; height and age combinations within the lines indicate the range of the original scarlet oak data.

Table 5.—White oak site index estimates by 2-foot height and 2-year age intervals^{1/} (McQuilkin 1974)

[illegible]

1/ All height and age combinations to the left of the line are within the range of the original data; combinations to the right of the line are extrapolations.

APPENDIX III

OAKREGEN: HP41C, a program for computing average stocking value and expected stump sprouting. This 1862 byte program can be run only on a Hewlett-Packard HP41CV or an HP41C with four memory modules added. A printer is desirable but not necessary. Clear the calculator of all programs, reserve 51 registers for data by pressing the following keys **[XEQ]** **[ALPHA]** **SIZE** **[ALPHA]** **051**, and then key in the OAKREGEN program listed below.

HOW TO USE THE PROGRAM

- A. To determine if advance reproduction alone is adequate press **[XEQ]** **[ALPHA]** **AR** **[ALPHA]** and you will be prompted to enter advance reproduction data. Press **[R/S]** after you enter each number. Use the following codes for aspect and slope position:

ASPECT	CODE	SLOPE POSITION	CODE
SW	1	Upper	1
SE & NW	2	Middle	2
NE	3	Lower	3

If there are no trees on a plot, press **[R/S]** when prompted for aspect.

After all data has been entered, calculate average stocking value by pressing **[XEQ]** **[ALPHA]** **SV** **[ALPHA]**.

- B. To determine the contribution of stump sprouts to future stocking press **[XEQ]** **[ALPHA]** **OV** **[ALPHA]** and enter overstory data when prompted. Press **[R/S]** after entering each number. After all data has been entered, calculate the number of stump sprouts expected per acre by pressing **[XEQ]** **[ALPHA]** **ST** **[ALPHA]**.

01*LBL "OV"	53 "NO 12-16?"	105 "17+:"	157 0
02*LBL 01	54 XEQ 90	106 XEQ 05	158 STO 22
03 FIX 3	55 "NO 17+?"	107 1.01701	159*LBL 11
04 0	56 XEQ 90	108 STO 50	160 1
05 0.01601	57 "SO 2-5?"	109 6.00901	161 ST+ 22
06 STO 50	58 XEQ 90	110 STO 49	162*LBL 39
07*LBL 03	59 "SO 6-11?"	111*LBL 10	163 "PLOT="
08 0	60 XEQ 90	112 3.5	164 ARCL 22
09 STO IND 50	61 "SO 12-16?"	113 XEQ IND 49	165 AVIEW
10 ISG 50	62 XEQ 90	114 ISG 50	166 23.02601
11 GTO 03	63 "SO 17+?"	115 CLD	167 STO 50
12 STO 48	64 XEQ 90	116 8.5	168 "ASPECT?"
13 "PLOT SIZE?"	65 "RO 2-5?"	117 XEQ IND 49	169 SF 01
14 PROMPT	66 XEQ 90	118 ISG 50	170 0
15 IND 17	67 "RO 6-12?"	119 14	171 XEQ 95
16 ARCL 17	68 XEQ 90	120 XEQ IND 49	172 "SLOPE?"
17 AVIEW	69 "RO 12-16?"	121 ISG 50	173 0
18 FIX 0	70 XEQ 90	122 19.5	174 XEQ 95
19 "STAND AGE?"	71 "RO 17+?"	123 XEQ IND 49	175 "HEIGHT?"
20 PROMPT	72 XEQ 90	124 ISG 50	176 .5
21 STO 18	73*LBL 90	125 ISG 49	177 FIX 1
22 ARCL 18	74 PROMPT	126 GTO 10	178 SF 00
23 AVIEW	75 ARCL X	127 CLA	179 XEQ 95
24 "SITE INDEX?"	76 AVIEW	128 ADV	180 0
25 PROMPT	77 ST+ IND 50	129 "SPROUTS PER AC."	181 "DIA?"
26 STO 19	78 0	130 AVIEW	182 .2
27 ARCL 19	79 ISG 50	131 "BO.NO.SO.RO."	183 SF 02
28 AVIEW	80 RTN	132 AVIEW	184 XEQ 95
29 ADV	81 GTO 02	133 1.01304	185 FIX 0
30*LBL 02	82*LBL "ST"	134 "2-5:"	186 RCL 23
31 ADV	83 RCL 00	135 XEQ 56	187 1
32 1.01601	84 1	136 2.01404	188 X=Y?
33 STO 50	85 -	137 "6-11:"	189 GTO 12
34 1	86 STO 00	138 XEQ 56	190 RCL 23
35 ST+ 00	87 "*****"	139 3.01504	191 2
36 RCL 00	88 AVIEW	140 "12-16:"	192 X=Y?
37 "POINT="	89 ADV	141 XEQ 56	193 GTO 13
38 ARCL 00	90 "STUMPS PER ACRE"	142 4.01604	194 RCL 23
39 AVIEW	91 AVIEW	143 "17+:"	195 3
40 0	92 "BO.NO.SO.RO."	144 XEQ 56	196 X=Y?
41 "BO 2-5?"	93 AVIEW	145 ADV	197 GTO 14
42 XEQ 90	94 CLA	146 "TOTAL SPROUTS="	198*LBL 38
43 "BO 6-11?"	95 1.01304	147 " " " "	199 "BAD ENTRY"
44 XEQ 90	96 "2-5:"	148 ARCL 48	200 AVIEW
45 "BO 12-16?"	97 XEQ 05	149 AVIEW	201 GTO 39
46 XEQ 90	98 2.01404	150 STOP	202*LBL 18
47 "BO 17+?"	99 "6-11:"	151*LBL "AR"	203 RCL 24
48 XEQ 90	100 XEQ 05	152 0	204 1
49 "NO 2-5?"	101 3.01504	153 STO 31	205 X=Y?
50 XEQ 90	102 "12-16:"	154 ADV	206 GTO 15
51 "NO 6-11?"	103 XEQ 05	155 "ADV REP"	207 RCL 24
52 XEQ 90	104 4.01604	156 AVIEW	208 2

209 X=Y?	261 -	313+LBL "SV"	365 ARCL X
210 GTO 16	262 LN	314 ADV	366 AVIEW
211 RCL 24	263 .2	315 "STOCKING VALUE "	367 STO IND 50
212 3	264 LN	316 "MEAN= "	368 ISG 50
213 X=Y?	265 X<>Y	317 RCL 31	369 RTN
214 GTO 17	266 /	318 RCL 22	370 RTN
215 GTO 38	267 1/X	319 1	371+LBL 60
216+LBL 19	268 100	320 -	372 CF 01
217 RCL 26	269 *	321 /	373 X=0?
218 SQRT	270+LBL 40	322 RND	374 GTO 40
219 5.1	271 RND	323 STO 32	375 GTO 70
220 *	272 "STOCKING VALUE="	324 ARCL X	376+LBL 96
221 RCL 25	273 "- "	325 AVIEW	377 CF 00
222 .7	274 ARCL X	326 29	378 X=0?
223 *	275 AVIEW	327 X<>Y	379 GTO 97
224 +	276 ST+ 31	328 X>Y?	380 SF 00
225 RCL 26	277 ADV	329 GTO 80	381 GTO 70
226 SQRT	278 GTO 11	330 RCL 32	382+LBL 97
227 RCL 25	279+LBL 12	331 ADV	383 0
228 *	280 -1	332 7.35	384 ST+ 31
229 -.444	281 STO 27	333 *	385 ARCL X
230 *	282 STO 28	334 CHS	386 AVIEW
231 +	283 GTO 18	335 221	387 FIX 0
232 -26.0731	284+LBL 13	336 +	388 GTO 40
233 +	285 0	337 "ADV REPRO"	389+LBL 65
234 RCL 27	286 STO 27	338 AVIEW	390 2.5
235 -.284	287 1	339 "NOT ADEQ."	391 X<>Y
236 *	288 STO 28	340 AVIEW	392 X>Y?
237 +	289 GTO 18	341 "MIN SPROUTS NEE"	393 X<>Y
238 RCL 28	290+LBL 14	342 "-DED= "	394 CF 02
239 .404	291 1	343 ARCL X	395 RTN
240 *	292 STO 27	344 AVIEW	396+LBL 68
241 +	293 0	345 STOP	397 10
242 RCL 29	294 STO 28	346+LBL 80	398 X<>Y
243 -1.1	295 GTO 18	347 "ADV REPRO"	399 X>Y?
244 *	296+LBL 15	348 AVIEW	400 X<>Y
245 +	297 -1	349 "ADEQUATE"	401 CF 00
246 RCL 30	298 STO 29	350 AVIEW	402 RTN
247 .646	299 STO 30	351 STOP	403+LBL 04
248 *	300 GTO 19	352+LBL 95	404 RCL IND 50
249 +	301+LBL 16	353 PROMPT	405 RCL 00
250 19	302 0	354 FS? 00	406 RCL 17
251 +	303 STO 29	355 GTO 96	407 *
252 CHS	304 1	356 FS? 01	408 1/X
253 E+X	305 STO 30	357 GTO 60	409 *
254 1	306 GTO 19	358+LBL 70	410 ARCL X
255 +	307+LBL 17	359 X<=Y?	411 ISG 50
256 1/X	308 1	360 X<>Y	412 GTO 04
257 .85	309 STO 29	361 FS? 00	413 AVIEW
258 *	310 0	362 XEQ 68	414 RTN
259 1	311 STO 30	363 FS? 02	415+LBL 05
260 X<>Y	312 GTO 19	364 XEQ 65	416 STO 50

417 XEQ 04	469 LN	521 LN	573 4.45376108
418 CLA	470 .2	522 .2	574 +
419 RTN	471 LN	523 LN	575 10+X
420+LBL 07	472 X<>Y	524 X<>Y	576 RCL 21
421 STO 20	473 /	525 /	577 X<>Y
422 1.1462	474 1/X	526 1/X	578 -
423 *	475 RCL IND 50	527 RCL IND 50	579 STO 21
424 .4323	476 *	528 *	580 .59484
425 +	477 RND	529 RND	581 *
426 STO 21	478 ST+ 48	530 ST+ 48	582 CHS
427 RCL 21	479 STO IND 50	531 STO IND 50	583 RCL 21
428 RCL 18	480 RTN	532 RTN	584 X+2
429 *	481+LBL 06	533+LBL 08	585 100
430 .00211455	482 STO 20	534 STO 20	586 /
431 *	483 1.1462	535 3.5	587 +
432 RCL 19	484 *	536 X<>Y	588 1.02390
433 X+2	485 .4323	537 X+Y?	589 +
434 .000511196	486 +	538 GTO 88	590 6.90428
435 *	487 STO 21	539 .46	591 +
436 +	488 RCL 18	540 RCL IND 50	592 CHS
437 RCL 18	489 *	541 *	593 E+X
438 -.0564873	490 -.00101597	542 RND	594 1
439 *	491 *	543 ST+ 48	595 +
440 +	492 RCL 19	544 STO IND 50	596 1/X
441 RCL 21	493 X+2	545 RTN	597 RCL 21
442 -.252517	494 .000415282	546+LBL 88	598 3
443 *	495 *	547 RCL 20	599 Y+X
444 +	496 +	548 1.1462	600 .00344484
445 2.23305	497 -.785279	549 *	601 *
446 +	498 +	550 .4323	602 RCL 21
447 CHS	499 CHS	551 +	603 X+2
448 E+X	500 E+X	552 STO 21	604 .161127
449 1	501 1	553 .23840565	605 *
450 +	502 +	554 *	606 CHS
451 1/X	503 1/X	555 RCL 21	607 +
452 RCL 21	504 RCL 21	556 X+2	608 RCL 21
453 1/X	505 1/X	557 .00278134	609 2.11955
454 18.3965	506 24.3594	558 *	610 *
455 *	507 *	559 CHS	611 +
456 -.847819	508 -2.5782	560 +	612 6.11437
457 +	509 +	561 RCL 21	613 CHS
458 CHS	510 CHS	562 1/X	614 +
459 E+X	511 E+X	563 8.2488119	615 CHS
460 1	512 1	564 *	616 E+X
461 +	513 +	565 CHS	617 1
462 1/X	514 1/X	566 +	618 +
463 *	515 *	567 RCL 21	619 1/X
464 .8875	516 .8875	568 LOG	620 *
465 *	517 *	569 5.68040348	621 .8875
466 1	518 1	570 *	622 *
467 X<>Y	519 X<>Y	571 CHS	623 1
468 -	520 -	572 +	624 X<>Y

625 -
 626 LN
 627 .2
 628 LN
 629 X<>Y
 630 /
 631 1/X
 632 RCL IND 50
 633 *
 634 RND
 635 ST+ 48
 636 STO IND 50
 637 RTN
 638+LBL 09
 639 STO 20
 640 RCL 18
 641 60
 642 X<>Y
 643 X>Y?
 644 GTO 99
 645 .86
 646 RCL IND 50
 647 *
 648 RND
 649 ST+ 48
 650 STO IND 50
 651 RTN
 652+LBL 99
 653 RCL 20
 654 3.5
 655 X<>Y
 656 X>Y?
 657 GTO 98
 658 4
 659 STO 20
 660+LBL 98
 661 RCL 20
 662 3
 663 Y+X
 664 .0032
 665 *
 666 CHS
 667 57.3
 668 +
 669 .00955
 670 *
 671 1
 672 X<>Y
 673 -
 674 LN
 675 .2
 676 LN

677 X<>Y
 678 /
 679 1/X
 680 RCL IND 50
 681 *
 682 RND
 683 ST+ 48
 684 STO IND 50
 685 RTN
 686+LBL 55
 687 .5
 688 RCL IND 50
 689 X<=Y?
 690 0
 691 ARCL X
 692 ISG 50
 693 GTO 55
 694 AVIEW
 695 RTN
 696+LBL 56
 697 STO 50
 698 XEQ 55
 699 CLA
 700 RTN
 701 .END.

LABELS

CAT 1

LBL'OV
 LBL'ST
 LBL'AR
 LBL'SV
 .END.

1862 BYTES

Sander, Ivan L.; Johnson, Paul S.; Rogers, Robert.

Evaluating oak advance reproduction in the Missouri Ozarks. Res. Pap. NC-251. St. Paul, MN: U.S. Department of Agriculture, Forest Service, North Central Forest Experiment Station; 1984. 16 p.

This guide presents a method for determining in advance of final harvest whether reproduction is adequate to reasonably ensure the regeneration of an oak stand in the Missouri Ozarks.

KEY WORDS: Quercus, stump sprouts, inventory, and final harvest.