



RESEARCH NOTE NC-199

NORTH CENTRAL FOREST EXPERIMENT STATION, FOREST SERVICE—U.S. DEPARTMENT OF AGRICULTURE

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A LOCAL NET VOLUME EQUATION FOR IOWA

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APPLICATION

As a part of the 1974 Forest Survey of Iowa, the Station's Forest Resources Evaluation Research Staff developed a merchantable tree volume equation and tables of coefficients for Iowa. They were developed for both board foot (International $\frac{1}{4}$ -inch rule) and cubic foot volumes, for several species and species groups of growing-stock trees.¹ The equation and the coefficients can be used on a digital computer or modern electronic desk calculator by industrial foresters, consulting foresters, or others in need of quick net-volume-per-tree estimates.

The only data needed to determine tree volumes in Iowa with the equation and coefficients are species, dbh, and site index. However, if site index measurements have not been taken, the average site index for the observations used in constructing tables 1 and 2 can be used.

To use the equation:

1. Select the appropriate table--table 1 for cubic foot volume or table 2 for board foot volume.
2. Obtain the species group number from table 3.
3. Substitute the appropriate coefficients A, B, and C; dbh; and site index from the table into the following equation.

$$\text{Volume} = A \cdot \text{site index} \cdot (1 - e^{-B \cdot \text{dbh}})^{\frac{1}{1-C}}$$

Where e is the well known mathematical constant for the base of the natural or Napierian

¹All live trees of commercial species except rough and rotten trees.

logarithm = 2.71828. For example the cubic foot volume for a 10.0 inch select white oak on a site with a site index of 55 is:

$$\begin{aligned} \text{Cubic volume} &= 39.90 \cdot 55 (1 - e^{-0.012 \cdot 10.0})^{\frac{1}{1-0.612}} \\ &= 7.97 \end{aligned}$$

DOCUMENTATION

Data collected on 6,158 trees from 500 plots representing a random sample of forest conditions in the State were used to develop these volume equations. Measurements taken were site index, tree class, dbh, merchantable height, and diameter of the stem outside bark at merchantable height. For sawtimber-size trees (9.0+ inches dbh for softwoods, 11.0+ inches for hardwoods), measurements were taken at both the sawtimber and pulpwood limits of merchantability. We also measured and estimated the volume of cull material (both in cubic feet and board feet) in each tree.

The net volume in these trees was then calculated using equations developed by Robert N. Stone² based on S. R. Gevorkiantz's "Composite Volume Tables for the Lake States."³ Stone's equations compute gross volume in a tree from three measurements--dbh, merchantable height, and diameter of the stem outside bark at merchantable height. The volume is

²Unpublished data on file at the North Central Forest Experiment Station, St. Paul, Minnesota.

³S. R. Gevorkiantz and L. R. Olsen. Composite volume tables for timber and their application in the Lake States. Lake States Tech. Bull. 1104, 51 p. 1955.

Table 1.--Cubic foot volume regression coefficients for growing stock trees, Iowa, 1974

$$VOL = A \cdot SI \cdot (1 - e^{-B \cdot dbh})^{\frac{1}{1-C}}$$

Species :	Coefficient			Average :		Standard :
group :	A	B	C	site	Observations	error of : R ²
number :	:	:	:	index :	estimate :	
					No.	Cu. Ft.
1-3	5.18	0.039	0.685	47	37	3.47 0.78
4	39.90	.012	.612	57	1,498	7.66 .87
5	75.96	.010	.629	60	772	9.58 .92
6	5.27	.032	.648	58	12	1.48 .99
7	7.42	.032	.679	61	246	8.83 .91
8	4.83	.034	.633	58	493	3.40 .88
9	94.92	.005	.532	62	217	10.05 .81
10-11	92.79	.006	.547	81	498	14.54 .91
12	4.67	.045	.724	70	206	6.84 .93
13	48.97	.013	.664	83	369	23.81 .90
14	18.48	.015	.589	69	91	4.45 .91
15	121.70	.007	.602	61	335	7.07 .88
16	39.96	.013	.624	65	599	8.09 .92
17	22.32	.016	.630	63	197	5.09 .86
18	125.20	.011	.669	66	64	3.97 .86
19	3.18	.051	.716	66	101	10.00 .88
20	2.28	.058	.714	71	175	4.32 .91
21	23.63	.013	.602	73	76	8.59 .79
22	39.67	.010	.604	67	172	11.19 .86

Table 2.--Board foot volume regression coefficients for growing stock trees, Iowa, 1974

Species :	Coefficient			Average :		Standard :
group :	A	B	C	site	Observations	error of : R ²
number :	:	:	:	index :	estimate :	
					No.	Bd. Ft.
1-3	13.57	0.050	0.671	46	14	26.29 0.55
4,6	100.10	.014	.583	57	980	61.16 .69
5	44.55	.026	.632	61	586	66.68 .81
7	23.32	.050	.734	59	137	99.70 .73
8	20.51	.035	.604	58	184	34.35 .62
9	8.42	.071	.690	63	139	78.31 .47
10-11	12.95	.059	.744	81	352	96.04 .77
12	10.12	.096	.846	72	108	69.25 .75
13	106.52	.020	.664	83	329	149.61 .84
14	79.77	.016	.590	68	41	39.68 .76
15	19.80	.049	.709	61	209	60.36 .65
16	21.23	.045	.707	63	319	72.84 .76
17	46.94	.024	.642	64	107	40.72 .68
18	7.41	.086	.777	66	26	43.23 .28
19	15.73	.038	.617	68	56	86.80 .61
20	9.46	.061	.713	73	93	43.56 .66
21	334.23	.006	.553	74	47	43.03 .76
22	40.05	.021	.599	68	90	63.96 .82

then corrected for differences in bark thickness between species and the field estimate of cull volume is subtracted to arrive at net volume. If tree heights are tallied while making a local cruise, measure bark thickness at the same time and use either the tables from Gevorkiantz and Olsen (1955) or Stone's equation, instead of the equations presented here, to compute volume.

Experience in working with volume-dbh relations suggested that the best mathematical model for this type of data was the Gompertz

Function: $Y = S \cdot B^{C^{D \cdot X}}$, $S = A \cdot SI$, and A, B, C and D are parameters. This is a special form of the more general Chapman-Richards

function: $Y = S(1 - e^{-B \cdot X})^{\frac{1}{1-C}}$, $S = A \cdot SI$, and A, B and C are parameters. In the past

the Chapman-Richards function was difficult to fit for volume-dbh data because the parameter C tended to approach the value 1. However, a new fitting procedure enabled us to use the Chapman-Richards function and solve for 3 instead of the 4 parameters of the Gompertz function. In the function, the dependent variable Y is net tree volume, the independent variable X is dbh, and the asymptote S is a function of site index ($S = A \cdot SI$).

The species groups used in the tables were primarily determined by the number of observations available for a group (a minimum number of observations are necessary to form an equation using least-squares estimates), and similarity of bole form of the species within a group. The number of observations, the standard error of estimate, and the R^2 for each regression estimate are shown in tables 1 and 2.

Table 3.--Species and species group numbers for Iowa trees

Species or species group	:	Scientific name	:	Number
<u>Softwoods</u>				
Red and white pine		<i>Pinus resinosa</i> <i>Pinus strobus</i>		1
Eastern redcedar		<i>Juniperus virginiana</i>		2
Other softwoods				3
<u>Hardwoods</u>				
Select white oaks		<i>Quercus alba</i> <i>Quercus bicolor</i> <i>Quercus macrocarpa</i> <i>Quercus michauxii</i> <i>Quercus muehlenbergii</i>		4
Select red oaks		<i>Quercus falcata</i> var. <i>pagodaefolia</i> <i>Quercus rubra</i>		5
Other white oaks		<i>Quercus lyrata</i> <i>Quercus prinus</i> <i>Quercus stellata</i> var. <i>stellata</i>		6
Other red oaks		<i>Quercus coccinea</i> <i>Quercus falcata</i> <i>Quercus imbricaria</i> <i>Quercus marilandica</i> <i>Quercus nigra</i> <i>Quercus palustris</i> <i>Quercus phellos</i> <i>Quercus velutina</i>		7

(Table 3 cont. on next page)

(Table 3 cont.)

Species or species group	Scientific name	Number
Hickory	<i>Carya cordiformis</i> <i>Carya glabra</i> <i>Carya illinoensis</i> <i>Carya laciniata</i> <i>Carya ovata</i> <i>Carya tomentosa</i>	8
Hard maple	<i>Acer nigrum</i> <i>Acer saccharum</i>	9
Soft maple	<i>Acer rubrum</i> var. <i>rubrum</i>	10
Tupelo and blackgum	<i>Nyssa aquatica</i> <i>Nyssa sylvatica</i> var. <i>sylvatica</i> <i>Nyssa sylvatica</i> var. <i>biflora</i>	11
Ash	<i>Fraxinus americana</i> <i>Fraxinus nigra</i> <i>Fraxinus pennsylvanica</i> <i>Fraxinus quadrangulata</i>	12
Cottonwood	<i>Populus deltoides</i> <i>Populus heterophylla</i>	13
Aspen	<i>Populus grandidentata</i> <i>Populus tremuloides</i>	14
Basswood	<i>Tilia americana</i>	15
Elm	<i>Ulmus alata</i> <i>Ulmus americana</i> <i>Ulmus rubra</i> <i>Ulmus thomasi</i>	16
Black walnut	<i>Juglans nigra</i>	17
Black cherry	<i>Prunus serotina</i>	18
Hackberry	<i>Celtis occidentalis</i>	19
Willow	<i>Salix nigra</i>	20
Birch	<i>Betula alleghaniensis</i> <i>Betula nigra</i> <i>Betula papyrifera</i> var. <i>papyrifera</i>	21
Other hardwoods	<i>Acer negundo</i> <i>Aesculus glabra</i> <i>Diospyros virginiana</i> <i>Gleditsia triacanthos</i> <i>Gymnocladus dioica</i> <i>Juglans cinerea</i> <i>Maclura pomifera</i> <i>Morus rubra</i> <i>Platanus occidentalis</i> <i>Robinia pseudoacacia</i> <i>Sassafras albidum</i>	22
Noncommercial species		23